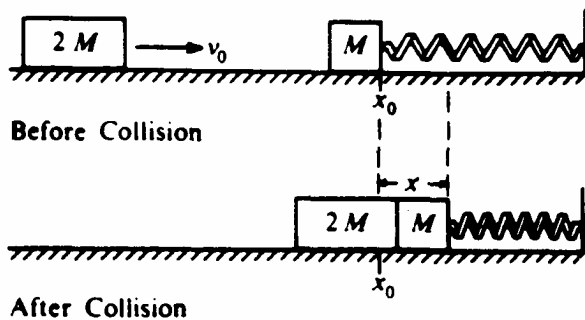


1981B2. A massless spring is between a 1-kilogram mass and a 3-kilogram mass as shown above, but is not attached to either mass. Both masses are on a horizontal frictionless table. In an experiment, the 1-kilogram mass is held in place and the spring is compressed by pushing on the 3-kilogram mass. The 3-kilogram mass is then released and moves off with a speed of 10 meters per second.

a. Determine the minimum work needed to compress the spring in this experiment.

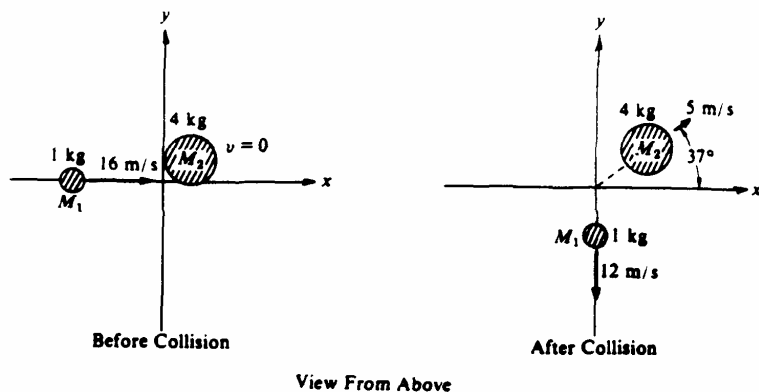
The spring is compressed again exactly as above, but this time both masses are released simultaneously.

b. Determine the final velocity of each mass relative to the table after the masses are released.



1983B2. A block of mass  $M$  is resting on a horizontal, frictionless table and is attached as shown above to a relaxed spring of spring constant  $k$ . A second block of mass  $2M$  and initial speed  $v_0$  collides with and sticks to the first block. Develop expressions for the following quantities in terms of  $M$ ,  $k$ , and  $v_0$ .

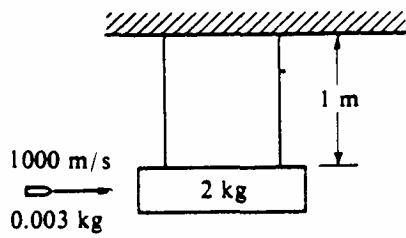
- $v$ , the speed of the blocks immediately after impact
- $x$ , the maximum distance the spring is compressed
- $T$ , the period of the subsequent simple harmonic motion



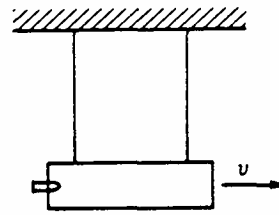
1984B2. Two objects of masses  $M_1 = 1$  kilogram and  $M_2 = 4$  kilograms are free to slide on a horizontal frictionless surface. The objects collide and the magnitudes and directions of the velocities of the two objects before and after the collision are shown on the diagram above. ( $\sin 37^\circ = 0.6$ ,  $\cos 37^\circ = 0.8$ ,  $\tan 37^\circ = 0.75$ )

	$M_1 = 1 \text{ kg}$		$M_2 = 4 \text{ kg}$	
	$p_x \left( \frac{\text{kg} \cdot \text{m}}{\text{s}} \right)$	$p_y \left( \frac{\text{kg} \cdot \text{m}}{\text{s}} \right)$	$p_x \left( \frac{\text{kg} \cdot \text{m}}{\text{s}} \right)$	$p_y \left( \frac{\text{kg} \cdot \text{m}}{\text{s}} \right)$
<b>Before Collision</b>				
<b>After Collision</b>				

- Calculate the x and y components ( $p_x$  and  $p_y$ , respectively) of the momenta of the two objects before and after the collision, and write your results in the proper places in the following table.
- Show, using the data that you listed in the table, that linear momentum is conserved in this collision.
- Calculate the kinetic energy of the two-object system before and after the collision.
- Is kinetic energy conserved in the collision?



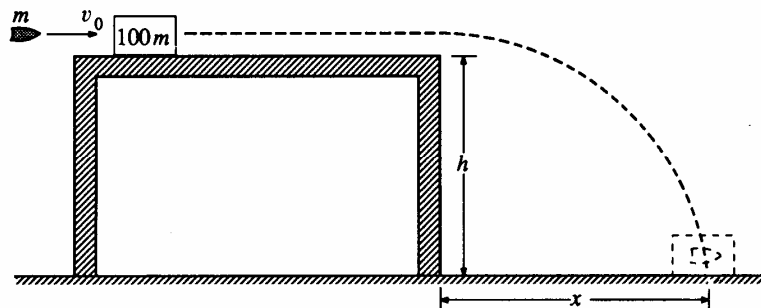
**Before Collision**



**Immediately After Collision**

1985B1. A 2-kilogram block initially hangs at rest at the end of two 1-meter strings of negligible mass as shown on the left diagram above. A 0.003-kilogram bullet, moving horizontally with a speed of 1000 meters per second, strikes the block and becomes embedded in it. After the collision, the bullet/ block combination swings upward, but does not rotate.

- Calculate the speed  $v$  of the bullet/ block combination just after the collision.
- Calculate the ratio of the initial kinetic energy of the bullet to the kinetic energy of the bullet/ block combination immediately after the collision.
- Calculate the maximum vertical height above the initial rest position reached by the bullet/block combination.



1990B1. A bullet of mass  $m$  is moving horizontally with speed  $v_0$  when it hits a block of mass  $100m$  that is at rest on a horizontal frictionless table, as shown above. The surface of the table is a height  $h$  above the floor. After the impact the bullet and the block slide off the table and hit the floor a distance  $x$  from the edge of the table. Derive expressions for the following quantities in terms of  $m$ ,  $h$ ,  $v_0$ , and appropriate constants:

- the speed of the block as it leaves the table
- the change in kinetic energy of the bullet-block system during impact
- the distance  $x$

Suppose that the bullet passes through the block instead of remaining in it.

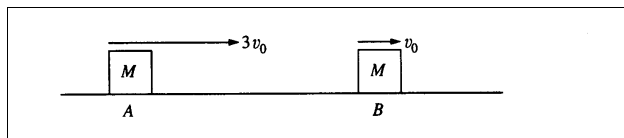
- State whether the time required for the block to reach the floor from the edge of the table would now be greater, less, or the same. Justify your answer.
- State whether the distance  $x$  for the block would now be greater, less, or the same. Justify your answer.

1992B2. A 30-kilogram child moving at 4.0 meters per second jumps onto a 50-kilogram sled that is initially at rest on a long, frictionless, horizontal sheet of ice.

- a. Determine the speed of the child-sled system after the child jumps onto the sled.
- b. Determine the kinetic energy of the child-sled system after the child jumps onto the sled.

After coasting at constant speed for a short time, the child jumps off the sled in such a way that she is at rest with respect to the ice.

- c. Determine the speed of the sled after the child jumps off it.
- d. Determine the kinetic energy of the child-sled system when the child is at rest on the ice.
- e. Compare the kinetic energies that were determined in parts (b) and (d). If the energy is greater in (d) than it is in (b), where did the increase come from? If the energy is less in (d) than it is in (b), where did the energy go?

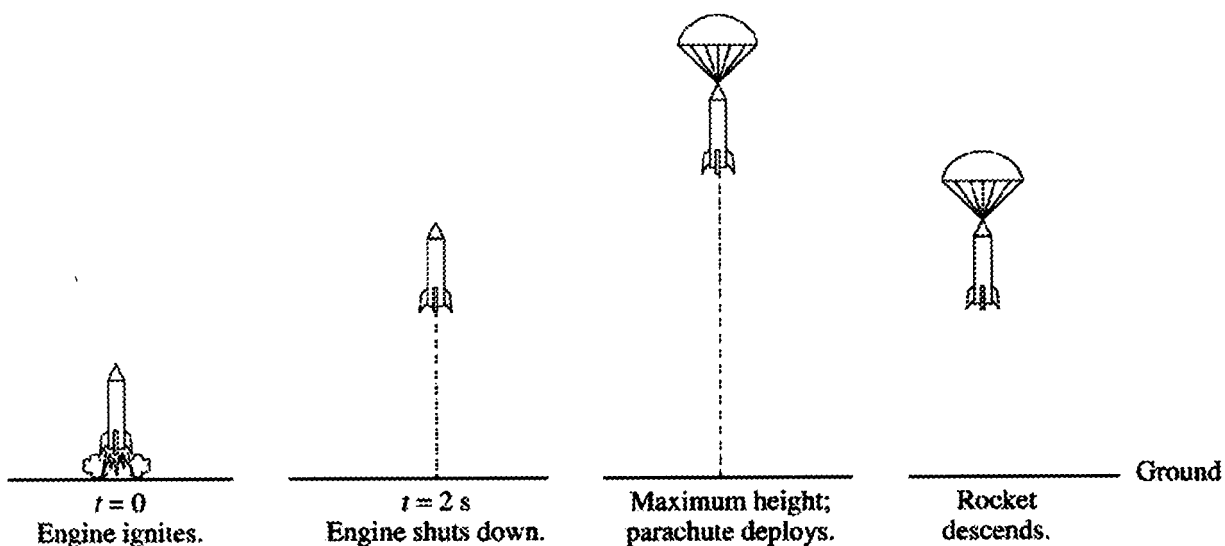


1996B1. (15 points) Two identical objects A and B of mass  $M$  move on a one-dimensional, horizontal air track. Object B initially moves to the right with speed  $v_0$ . Object A initially moves to the right with speed  $3v_0$ , so that it collides with object B. Friction is negligible. Express your answers to the following in terms of  $M$  and  $v_0$ .

- a. Determine the total momentum of the system of the two objects.
- b. A student predicts that the collision will be totally inelastic (the objects stick together on collision). Assuming this is true, determine the following for the two objects immediately after the collision.
  - i. The speed
  - ii. The direction of motion (left or right)

When the experiment is performed, the student is surprised to observe that the objects separate after the collision and that object B subsequently moves to the right with a speed  $2.5v_0$ .

- c. Determine the following for object A immediately after the collision.
  - i. The speed
  - ii. The direction of motion (left or right)
- d. Determine the kinetic energy dissipated in the actual experiment.



**Note:** Figures not drawn to scale.

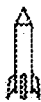
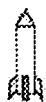
2002B1. A model rocket of mass  $0.250 \text{ kg}$  is launched vertically with an engine that is ignited at time  $t = 0$ , as shown above. The engine provides an impulse of  $20.0 \text{ N}\cdot\text{s}$  by firing for  $2.0 \text{ s}$ . Upon reaching its maximum height, the rocket deploys a parachute, and then descends vertically to the ground.

(a) On the figures below, draw and label a free-body diagram for the rocket during each of the following intervals.

i. While the engine is firing

ii. After the engine stops, but before the parachute is deployed

iii. After the parachute is deployed



(b) Determine the magnitude of the average acceleration of the rocket during the  $2 \text{ s}$  firing of the engine.

(c) What maximum height will the rocket reach?

(d) At what time after  $t = 0$  will the maximum height be reached?